

Chapter 13 - Universal Gravitation

Physics 206

Group 1 Problems:

Problem 1:

$$v_2 = \frac{r_1}{r_2} v_1$$

Problem 2:

- (a) $\Delta E = 3.27 \times 10^7 \text{ J} = 9.07 \text{ kW} \cdot \text{hr}$
(b) Cost = \$544

Problem 3:

$$\begin{aligned} a &= 1.45 \times 10^{14} \text{ m} \\ &= 1.45 \times 10^{11} \text{ km } 100 \text{ times larger than Pluto's distance} \\ &= 0.0153 \text{ light years} \end{aligned}$$

Problem 4:

$$W = \frac{GMm}{4r_0}$$

Problem 5:

$$g = 2.027 \times 10^{-4} \text{ m/s}^2$$

Group 2 Problems:

Problem 6:

$$\begin{aligned} \text{(a)} \quad F_g &= \frac{16\pi^2 m \left(\frac{D}{2} + h\right)^3}{D^2 T^2} \\ \text{(b)} \quad F_g &= \frac{16\pi^2 m \left(\frac{D}{2} + h\right)^3}{D^2 T^2} - \frac{2m\pi^2 D}{T_D^2} \end{aligned}$$

Problem 7:

$$v_f = \sqrt{GM_M \frac{R_M + H}{R_M(R_M + H)}}$$

Problem 8:

$$\begin{aligned} \text{(a)} \quad F &= \frac{GM_1 m_3}{x^2} - \frac{GM_2 m_3}{(d-x)^2} \\ \text{(b)} \quad x &= \frac{M_1(1 - \sqrt{M_2/M_1})d}{M_1 - M_2} \end{aligned}$$

Problem 9:

$$r_A = 4.60 \times 10^7 \text{ m}$$

Problem 10:

$$\begin{aligned} \text{(a)} \quad a_X &= 12 \text{ AU} \\ \text{(b)} \quad F_{G,X} &= 400 \text{ lbs} \end{aligned}$$

Group 3 Problems:

Problem 11:

$$\begin{aligned} \text{(a)} \quad \vec{F} &= Gm_1 \sqrt{\frac{m_3^2}{a^4} + \frac{m_2^2}{b^4}} \\ \text{(b)} \quad U &= -\frac{Gm_1 m_2}{b} - \frac{Gm_1 m_3}{a} - \frac{Gm_2 m_3}{\sqrt{a^2 + b^2}} \\ \text{(c)} \quad W_{ext} &= \frac{Gm_1 m_2}{b} + \frac{Gm_2 m_3}{\sqrt{a^2 + b^2}} \\ \text{(d)} \quad L &= m_3 \sqrt{Gam_1} \end{aligned}$$

Problem 12:

$$\vec{F} = -\frac{GM_1 m_3 (x - x_1)}{(x - x_1)^{3/2}} \hat{x} - \frac{GM_2 m_3 (x - x_2)}{(x - x_2)^{3/2}} \hat{x}$$

Problem 13:

$$\theta = 70.9 \text{ degrees}$$